# Refraction from an irregular surface: **Delay-Time Method**



Define *delay time* as the time the ray traveled in layer 1 along a "slant path", less the time it would have taken to travel the horizontal distance (AB) at velocity  $V_2$ . Thus, the total delay time  $\tau_{EG}$  traveling from E to G (or G to E) is

$$au_{EG} = t_R - \frac{y}{V_2}$$
, where  $t_R$  is total travel time.

Delay time under E:  $\tau_E = t_R - \frac{y}{V_2} - \tau_G = \frac{EB}{V_1} - \frac{AB}{V_2}$ 

$$\tau_E = \frac{h_E}{V_1 \cos i_c} - \frac{h_E \tan i_c}{V_2} = h_E \frac{\sqrt{V_2^2 - V_1^2}}{V_1 V_2} \Longrightarrow h_E = \tau_E \frac{V_1 V_2}{\sqrt{V_2^2 - V_1^2}}$$

(This is half of the "time intercept" on our t-x plots!)



## **Key Assumptions**

 $\tau_{H}$  from E  $\approx \tau_{H}$  from G

Refractor surfaces are planar \* Beneath source \* Beneath geophone

Refractor surface undulations are small compared to its extent - i.e., long wavelength, with

dips <10°

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$$t_{EH} + t_{GH} \rightarrow \tau_{H} = \frac{t_{EH} + t_{GH} - t_{EG}}{2}$$
  $h_{H} = \tau_{H} \frac{V_{1}V_{2}}{\sqrt{V_{2}^{2} - V_{1}^{2}}}$ 

Problem however: to get  $h_H$  from  $\tau_H$ , we need to know  $V_2$ ! However, we have:

$$t_{EH} - t_{GH} = \left(\tau_E + \tau_H + \frac{x}{V_2}\frac{1}{y}\right) \left(\tau_G + \tau_H + \frac{y - x}{V_2}\frac{1}{y}\right) = \tau_E - \tau_G - \frac{y}{V_2} + \frac{2x}{V_2}$$

 $(\Rightarrow$  a line with slope  $2/V_2!$ )

# **Delay Time, or "Plus-Minus" Method**



- Plot  $t_{1i}$   $t_{2i}$  vs  $x_i$  for SP1, SP2 and all geophones i.
- Calculate  $V_2$  from slope of the line fit  $(V_2 = 2/m)$ .
- At each geophone *i*, calculate thickness as:

$$h_i = \left(\frac{t_{1i} + t_{2i} - t_{12}}{2}\right) \frac{V_1 V_2}{\sqrt{V_2^2 - V_1^2}}$$



# **Key Field considerations**

#### \* Local Geology \* Spread-lengths

- bedrock depths of 50-70 m
- $L_{min}$  +  $n.\Delta x_{take-out}$
- Typically, *L<sub>min</sub>*~ 200 *m*, *n* > 3

### \* Geophone coupling

- Auger 1 m deep holes
- Fill with water to saturate

## \* Elevation effects

- Minimize OR use elevation corrections
- \* Wind
- calm day
- night-time

## \* Continual Traffic

- vehicles, trains
- pedestrians

### \* Source

- Hammer or shotgun?
- \* Signal Attenuation\* Noise filtering